

# *The theory of Galactic Chemical Evolution*

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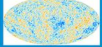





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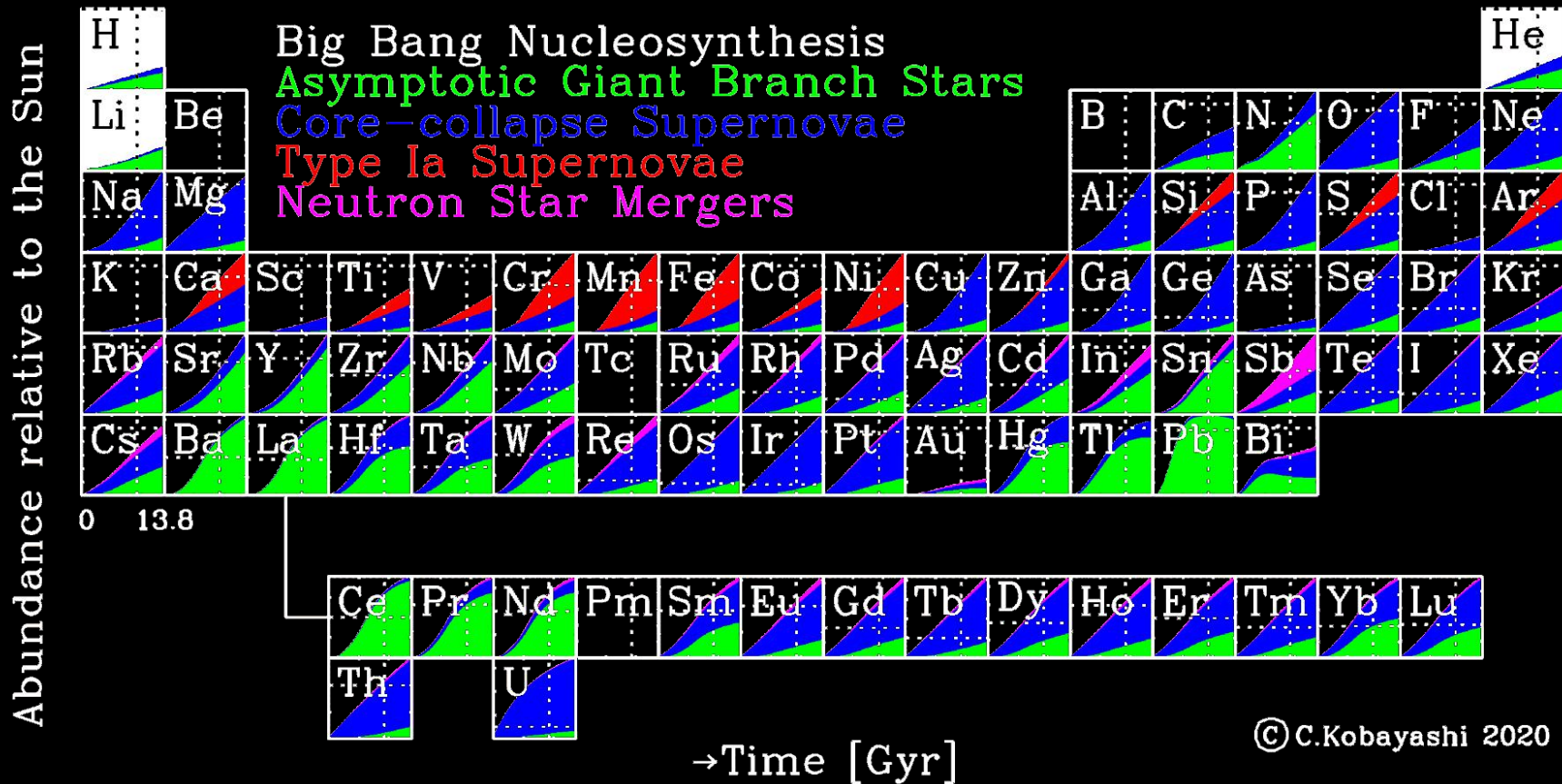
**ELTE**  
EÖTVÖS LORÁND  
TUDOMÁNYEGYETEM

# FORMATION OF THE ELEMENTS

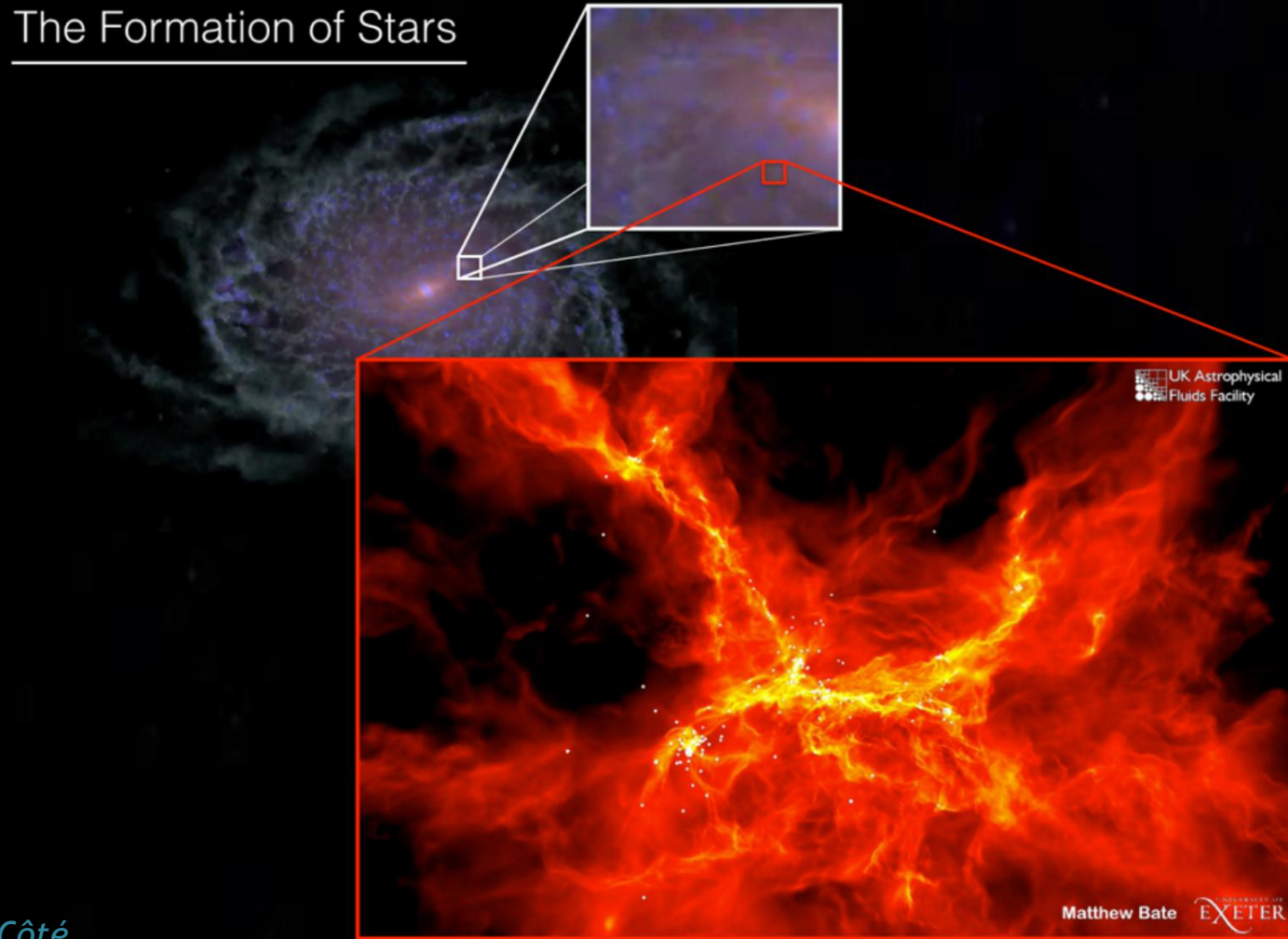
# The origin of the elements: schematically

1 H	big bang fusion 										cosmic ray fission 					2 He	
3 Li	4 Be	merging neutron stars 					exploding massive stars 					5 B	6 C	7 N	8 O	9 F	10 Ne
11 Na	12 Mg	dying low mass stars 					exploding white dwarfs 					13 Al	14 Si	15 P	16 S	17 Cl	18 Ar
19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr
37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe
55 Cs	56 Ba		72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn
87 Fr	88 Ra																
			57 La	58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu
			89 Ac	90 Th	91 Pa	92 U											


# The origin of the elements: ... over time



# The Formation of Stars



UK Astrophysical  
Fluids Facility

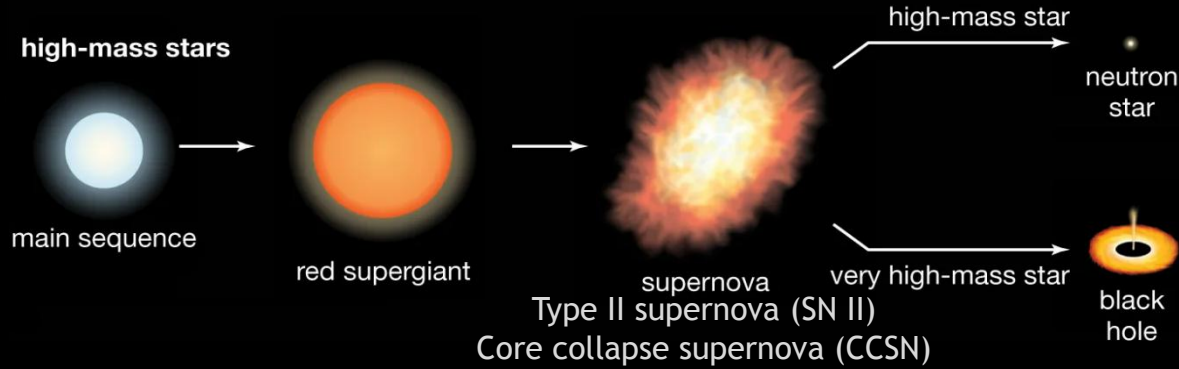
Matthew Bate 

Slide from B. Côté



# Evolution of stars

- High-mass stars ( $> 8 M_{\odot}$ )



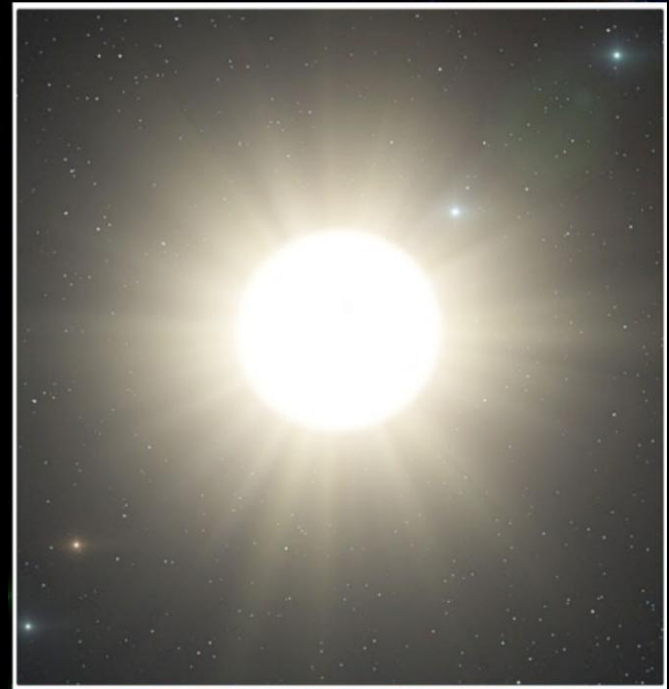
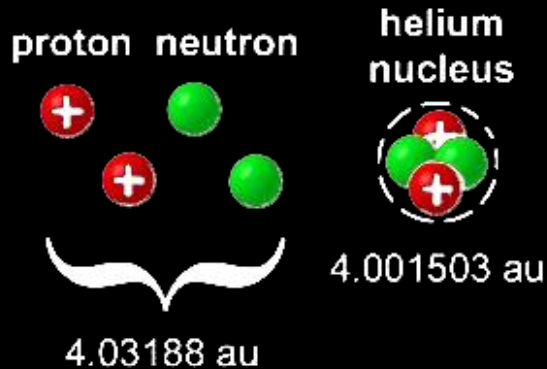
- Low- and intermediate mass stars ( $0.8-8 M_{\odot}$ )



# The Process of Nuclear Fusion

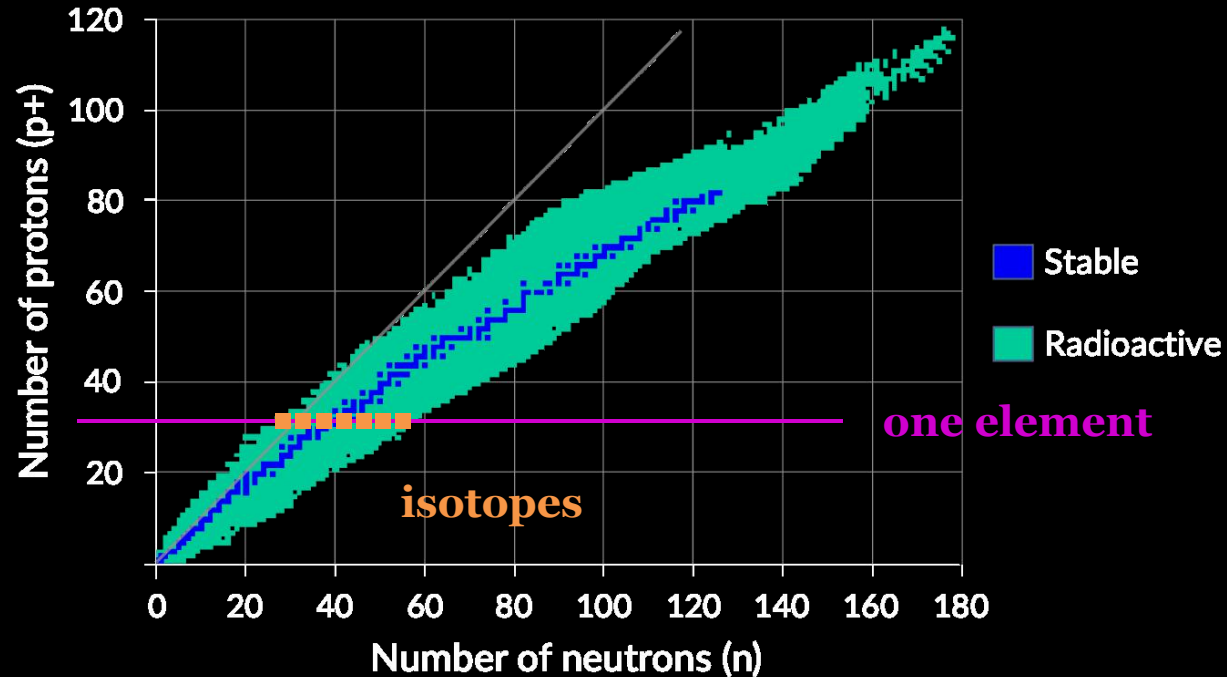
Each year, the Sun produce 25 millions of millions more energy than what humanity consumes in a year.

$$E = mc^2$$



# The nuclear chart: neutron captures

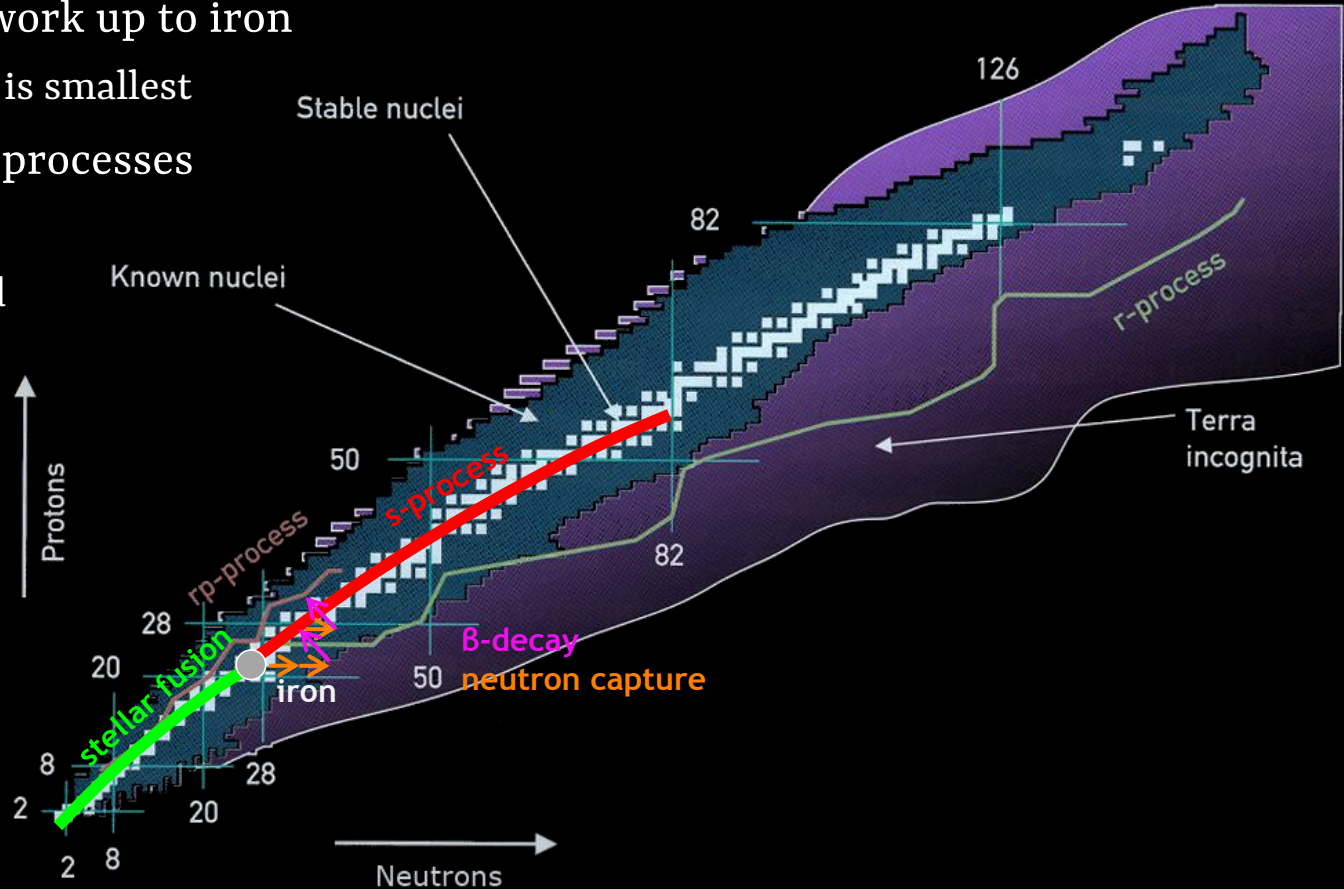
- Nuclear chart: number of protons vs. neutrons
- Valley of stability
- Unstable nuclei will  $\beta$ -decay towards stability





# The nuclear chart: neutron captures

- Fusion can only work up to iron
  - Binding energy is smallest
- Neutron capture processes
  - *s*-process: slow
  - *r*-process: rapid
  - *i*-process: intermediate

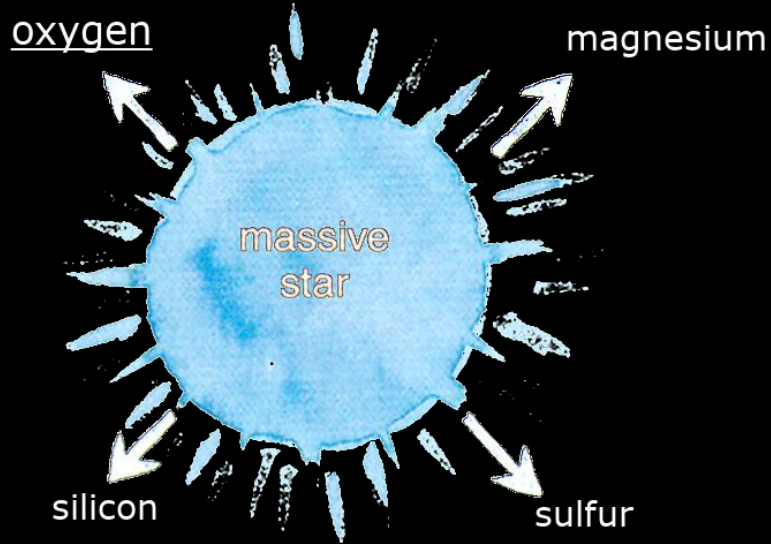


# Elemental synthesis of stars

- High-mass stars ( $> 8 M_{\odot}$ )
  - Stellar wind: elements from the main sequence
  - SN II/CCSN:  $\alpha$ -elements, elements beyond iron (+  $r$ -process?)
  - Neutron stars / black holes - compact object mergers (+?):  $r$ -process
- Low- and intermediate mass stars ( $1.2-8 M_{\odot}$ )
  - Red giant and AGB stars: stellar winds, dust formation  $\rightarrow$  C, N, F, Na, ... +  $s$ -process
  - White dwarf - SN Ia: iron-peak elements (Fe, Ni, Co,...)
- Low-mass stars ( $< 1.2 M_{\odot}$ ): no relevant contribution

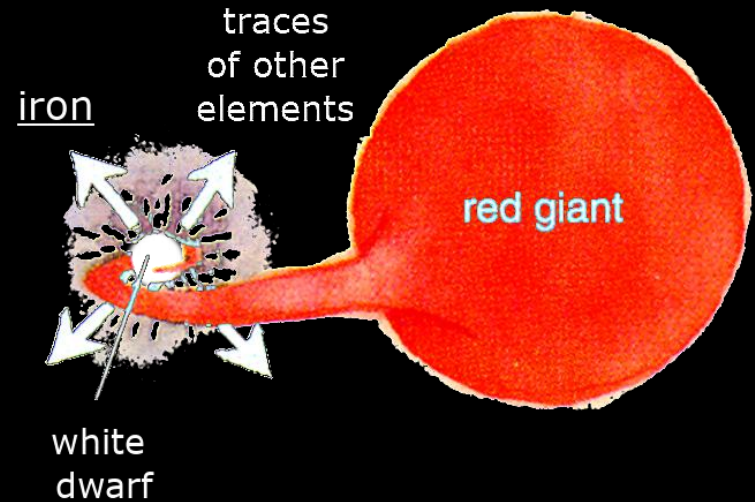
# The $\alpha$ -elements and iron

## TYPE II SUPERNOVA



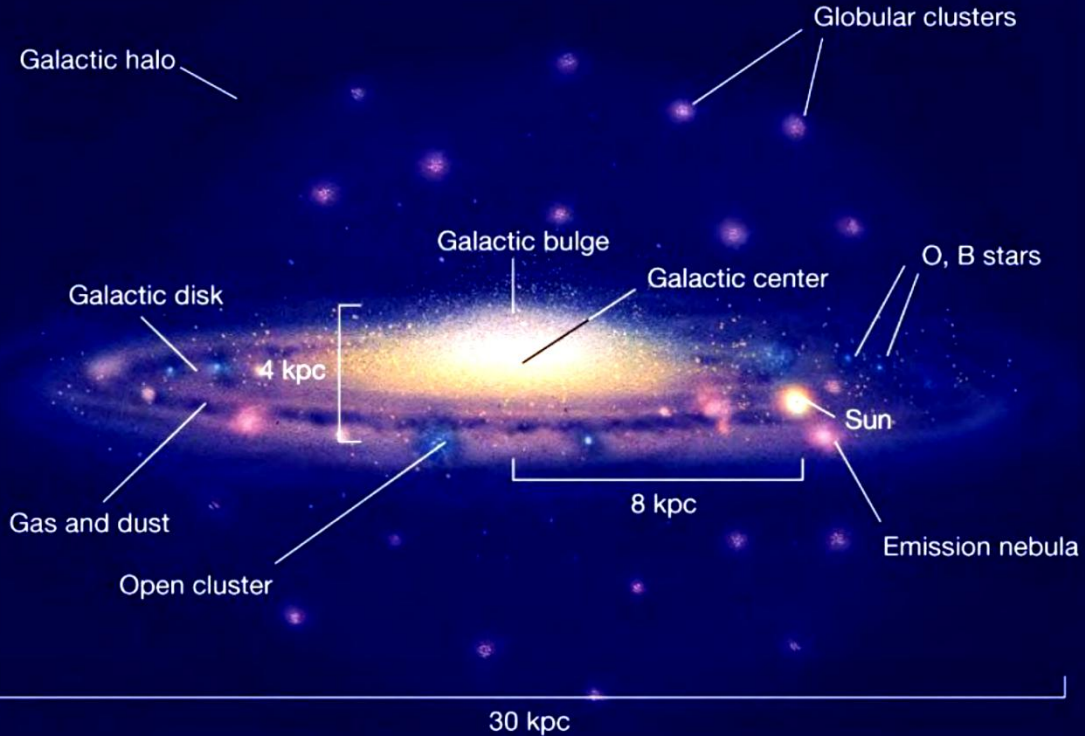
brief life (millions of years)

## TYPE IA SUPERNOVA



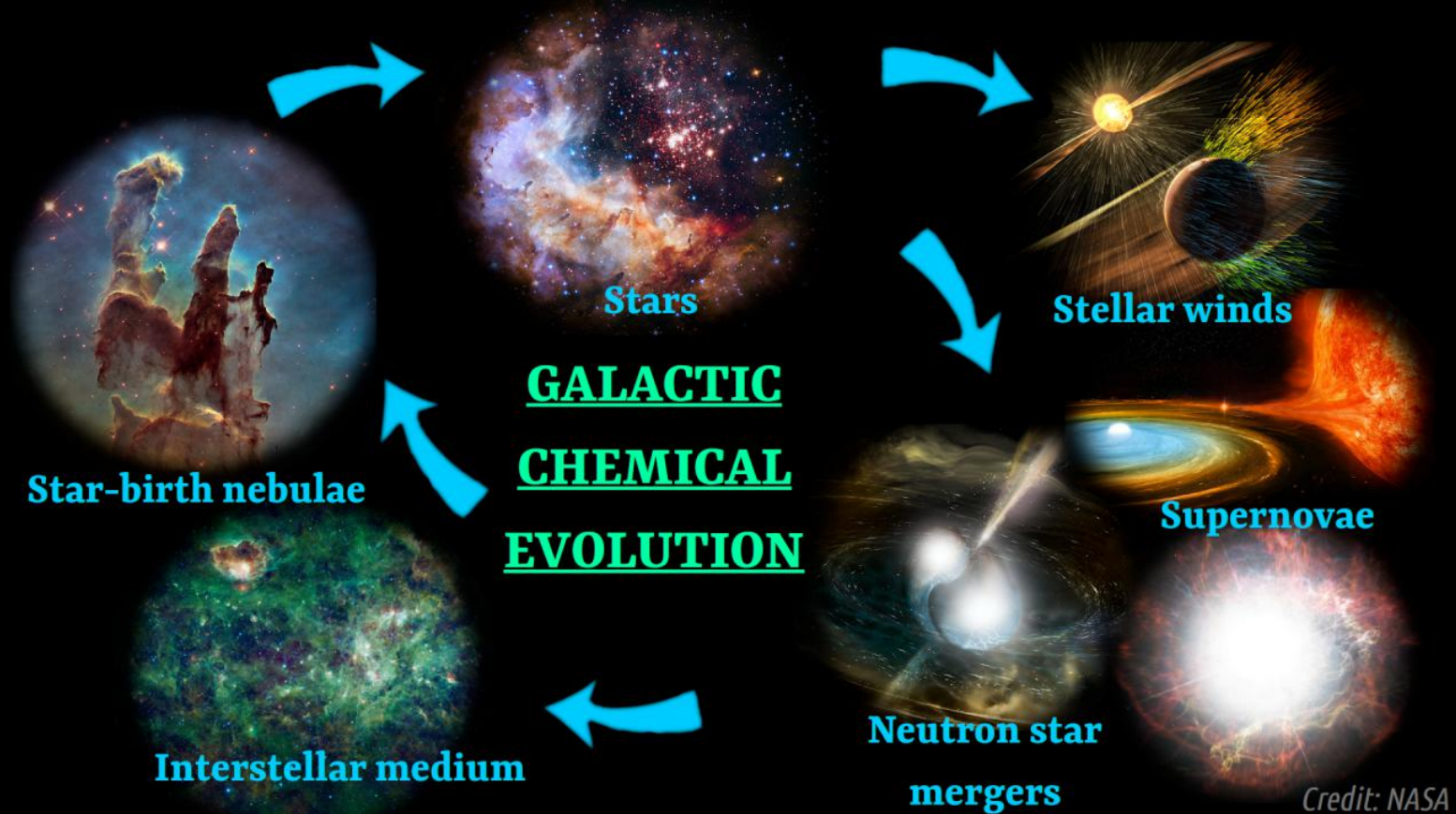
long life (billions of years)

# How does a galaxy look like?

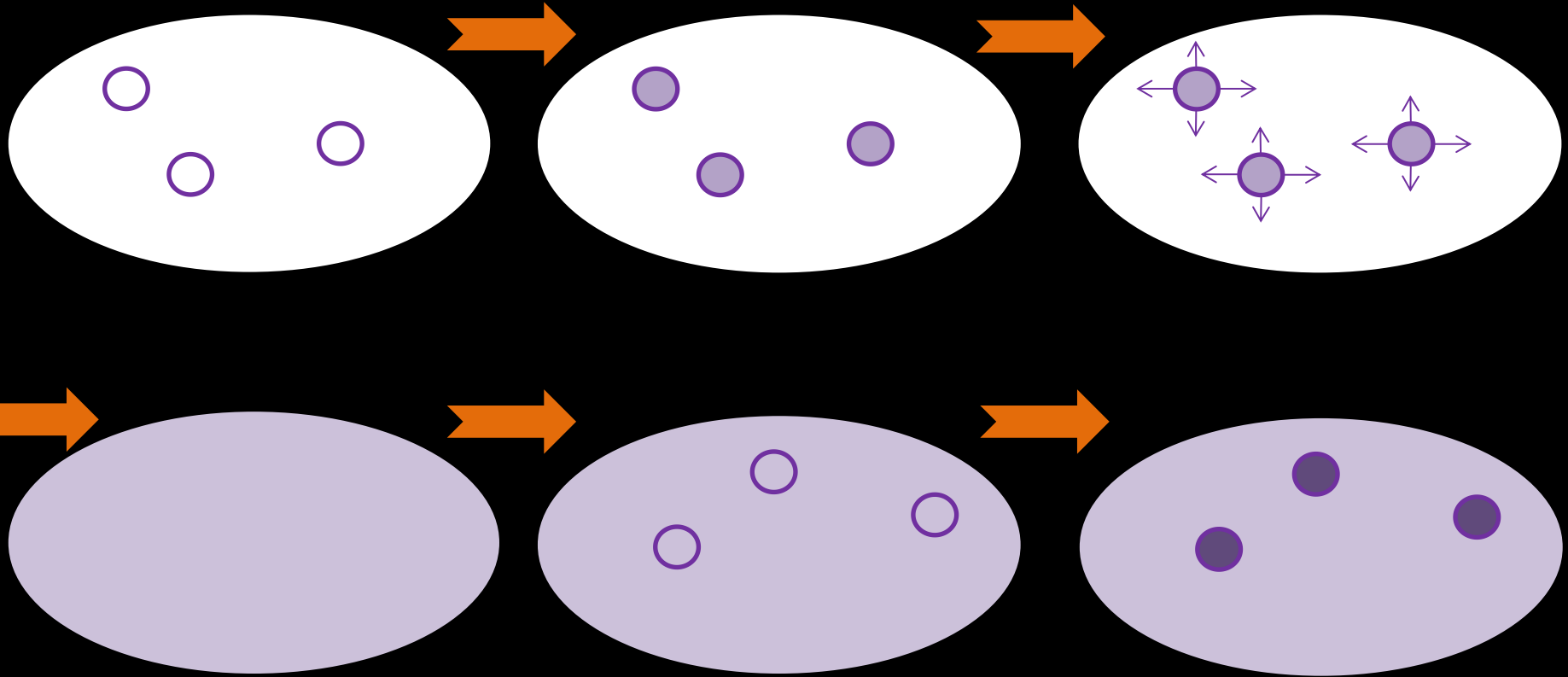


1 pc = 3.26 ly =  $3.086 \times 10^{13}$  Km

# Galactic Chemical Evolution (GCE)



# Generation of stars



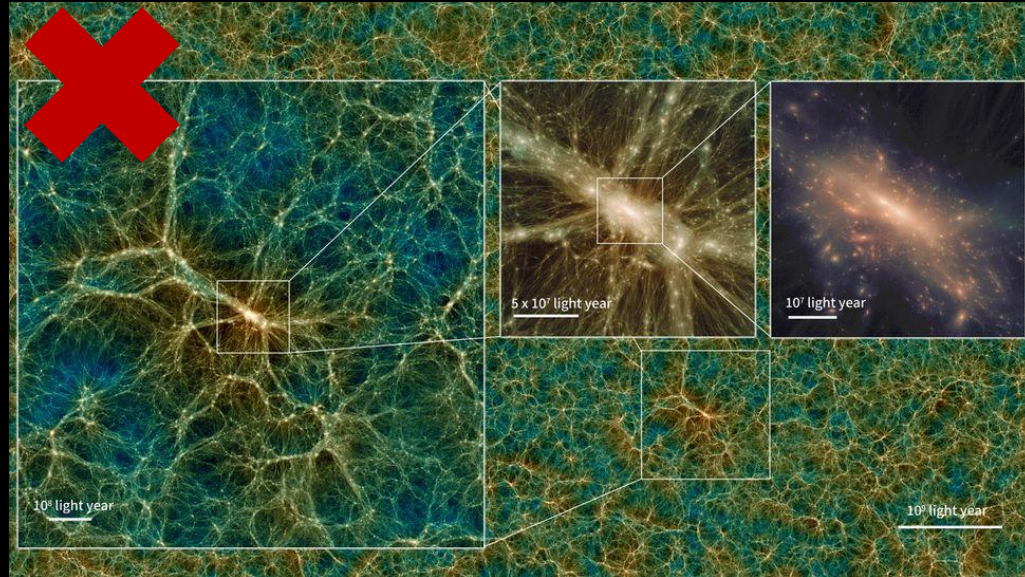


# **GCE MODELS: TYPES, OBSERVABLES**

# Principles of simple GCE

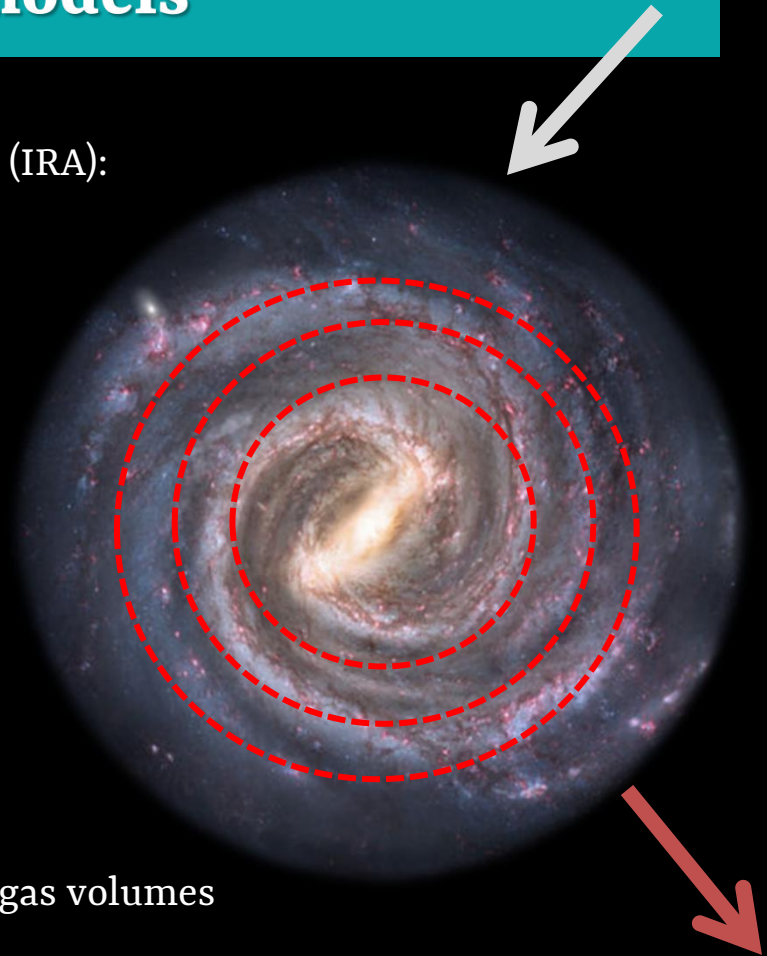
- Galaxy simulations: cosmological / chemical evolution
- The average evolution of the interstellar gas (homogeneously mixed)
- Aim: **reproduce observables** by the fine-tuning of the models and their parameters

*Cosmological simulation*

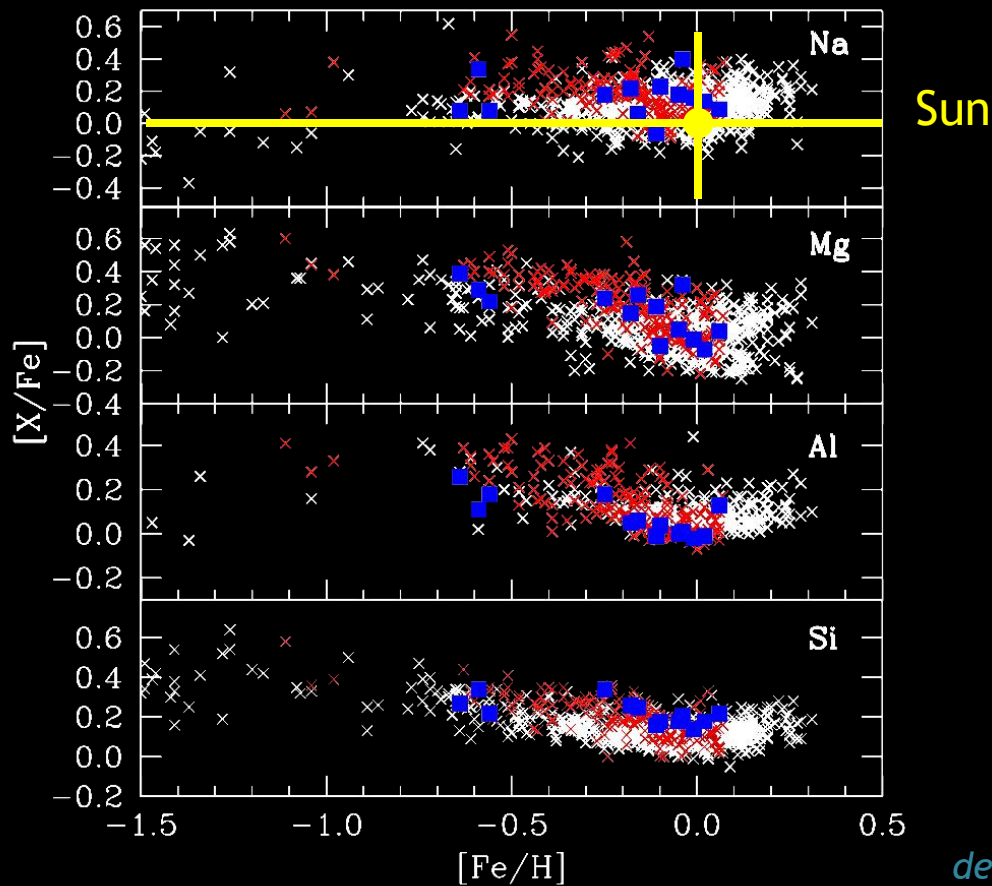


# Types of GCE models

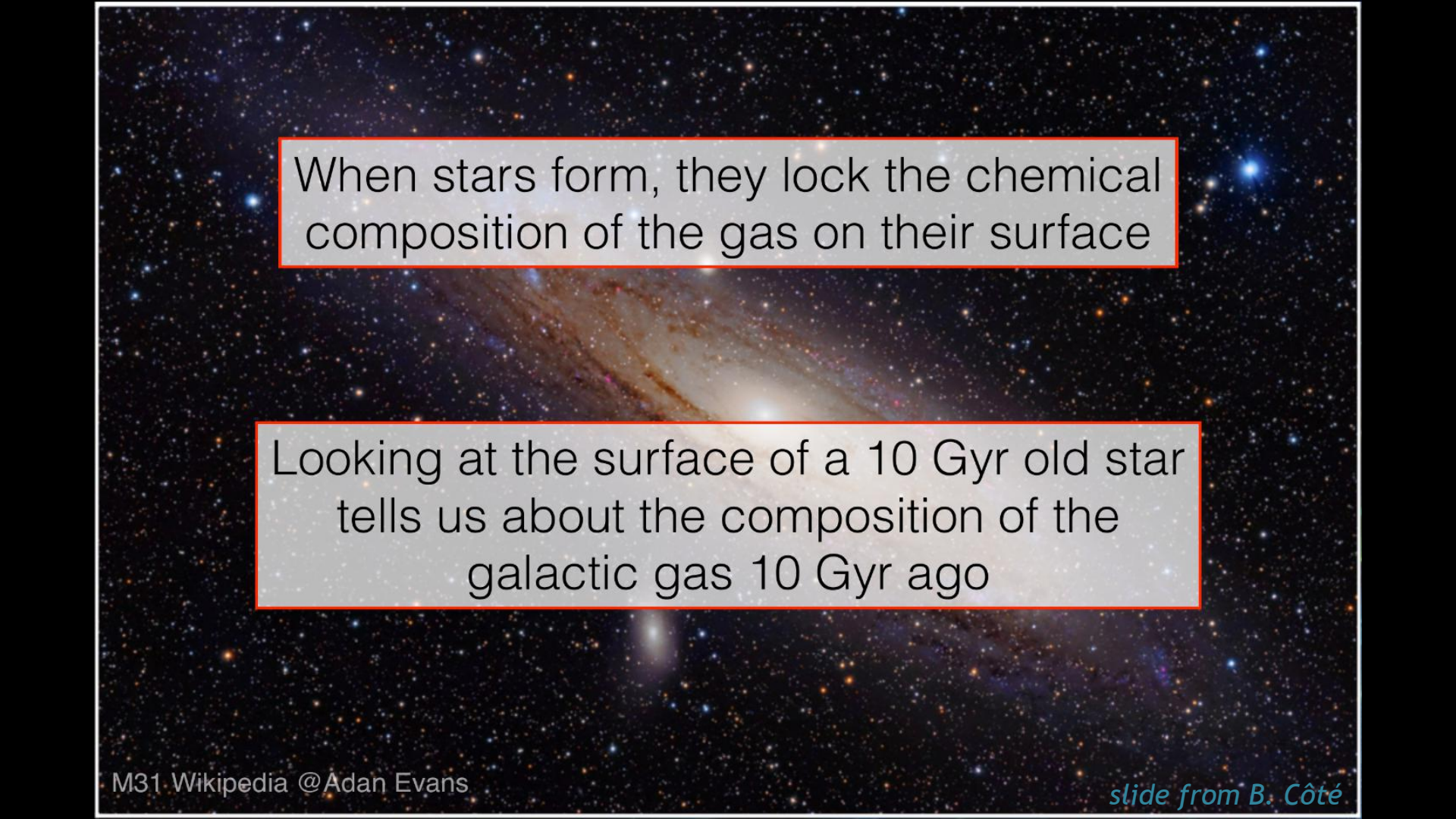
- **Analytic/numerical**
  - Analytic: Instantaneous Relaxation Approximation (IRA):  
low-mass stars live forever;  
high-mass stars explode/implode instantly
  - Numerical (the magnitude of the timestep!)
- **Closed/open system**
  - Interaction with environment: gas in- & outflows
  - G-dwarf problem: too few metal-poor G stars
- **Number of zones or components**
  - Radial zones (rings)
  - Or components: disk, halo etc.
- **Homogeneous/inhomogeneous mixing**
  - Instantaneous gas mixing or evolution of multiple gas volumes



# Stellar abundances





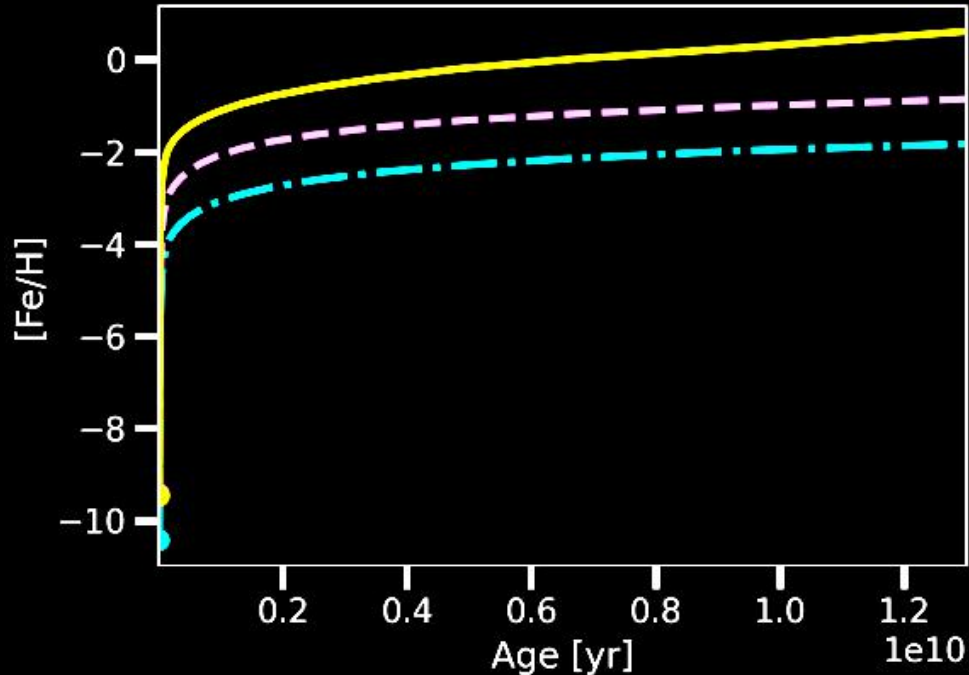


When stars form, they lock the chemical composition of the gas on their surface

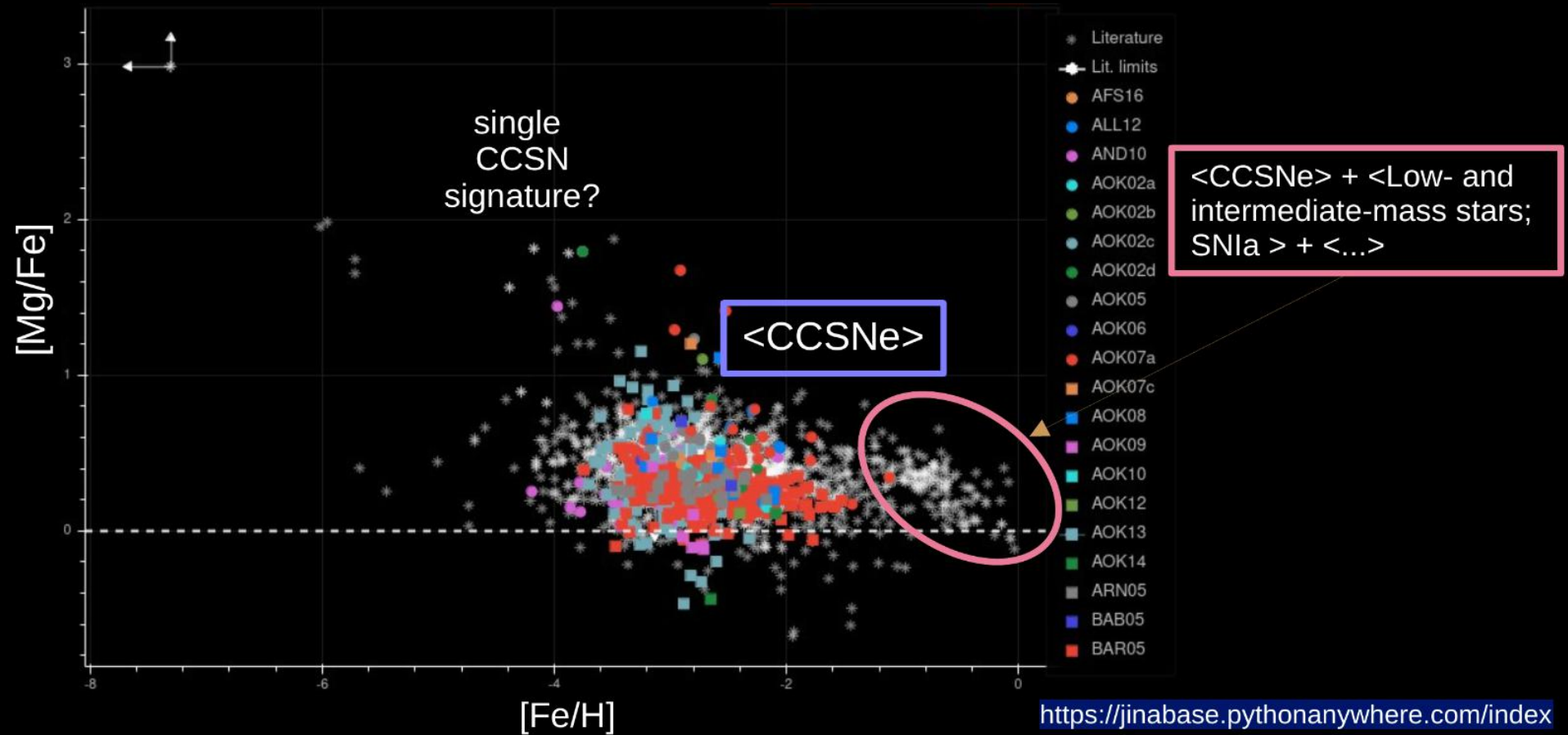
Looking at the surface of a 10 Gyr old star tells us about the composition of the galactic gas 10 Gyr ago

# Age or metallicity?

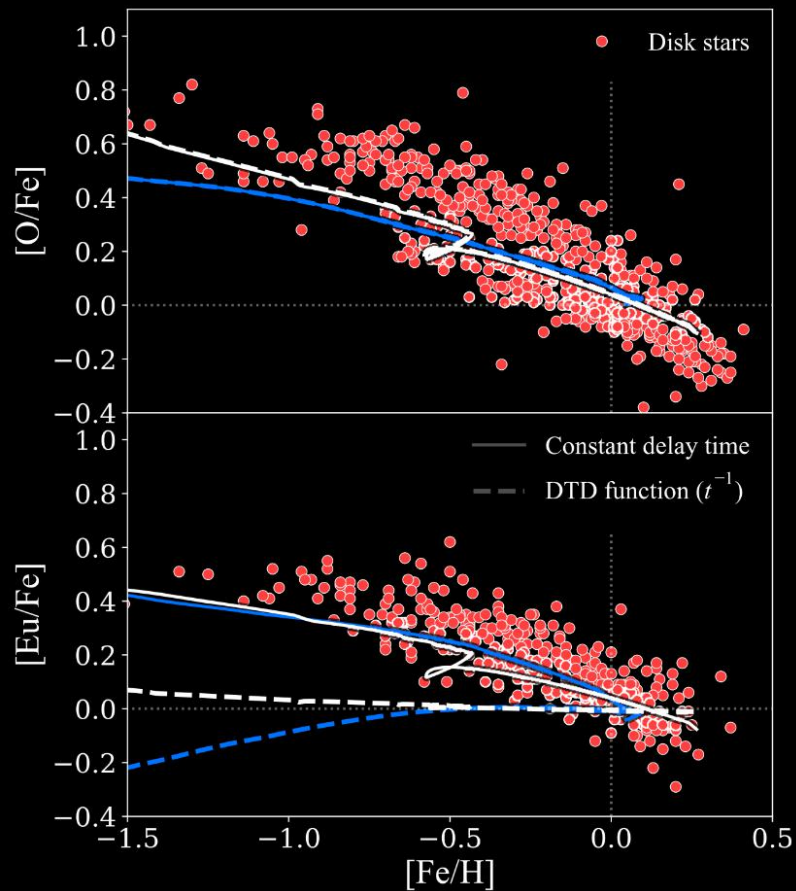
- Measuring the age of the stars is hard - asteroseismology
- Metallicity is easily observed, and it should increase for younger stars!





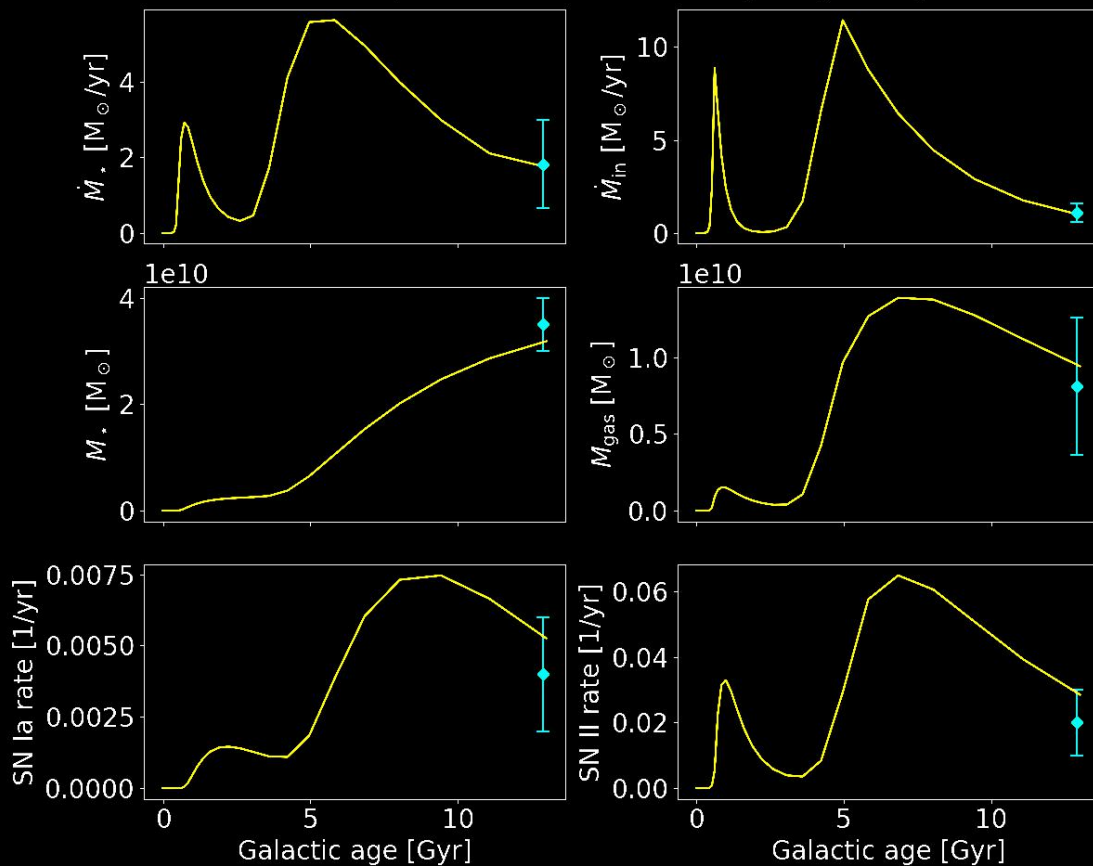


# Stellar abundances

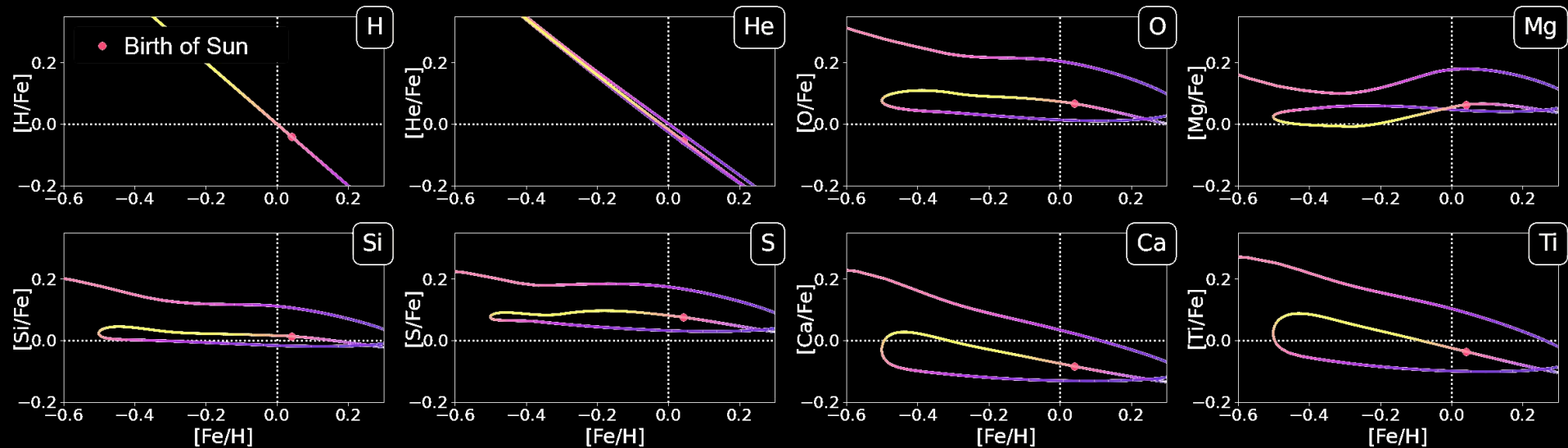


# Global parameters today

Global parameters of the Milky Way today



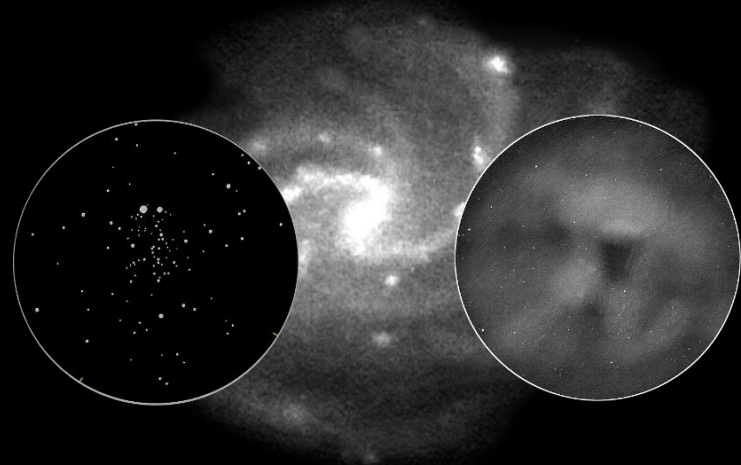
# Composition at the birth of the Sun



# THE MAIN EQUATION OF GCE

# What is a galaxy made of? - GCE perspective

- **Interstellar matter (ISM)**
  - New stars are born from it
  - It is becoming more and more enriched in heavy elements
- **Stars**
  - Enclose the ISM (stellar remnants enclose it for ever)
  - Synthesize heavy elements during life
- **Dark matter**
  - Increases the mass → more gas inflow
- **Environment, companions**
  - Interaction: what mass, what composition?



*M33: Kiss Péter  
Bagoly-halmaz: Sánta Gábor  
Rózetta-köd: Kernya János*



# The main equation

- The change of mass of the gas:  $dM_{\text{gas}} = dM_{\text{in}} - dM_{*} + dM_{\text{rec}} - dM_{\text{out}}$

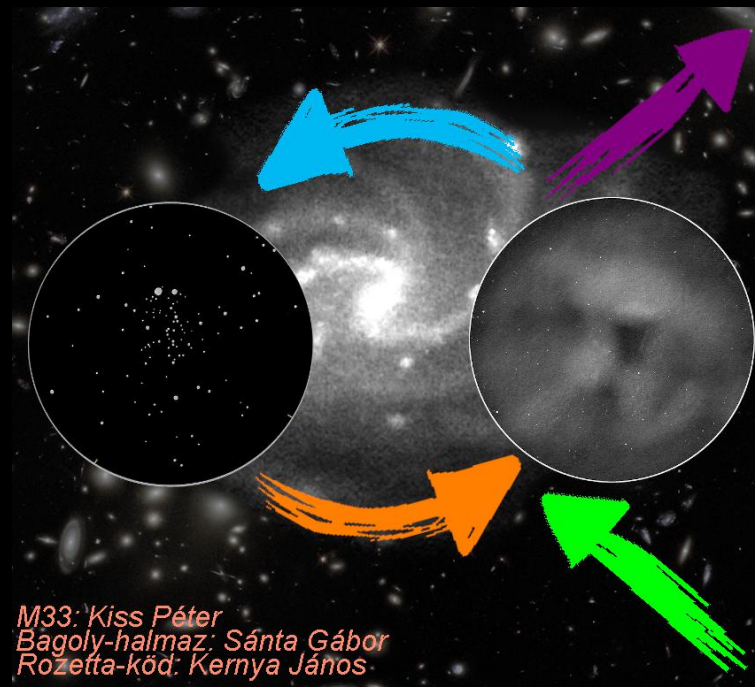
1.  $dM_{\text{in}}$  inflows from the intergalactic space

2.  $dM_{*}$  mass enclosed in newly-born stars

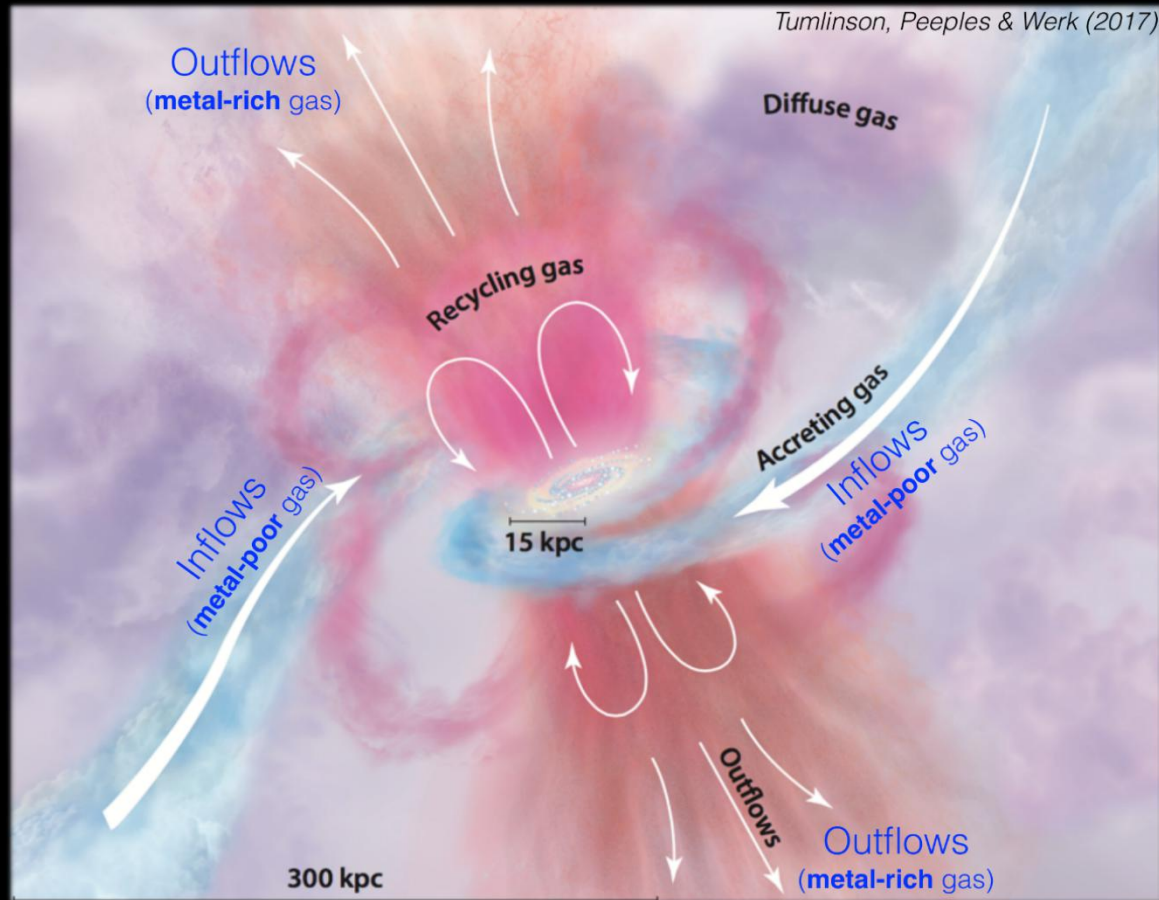
3.  $dM_{\text{rec}}$  mass recycled to the ISM by stars, supernovae, etc.

4.  $dM_{\text{out}}$  gas outflows to the intergalactic space

- True independently for all isotopes



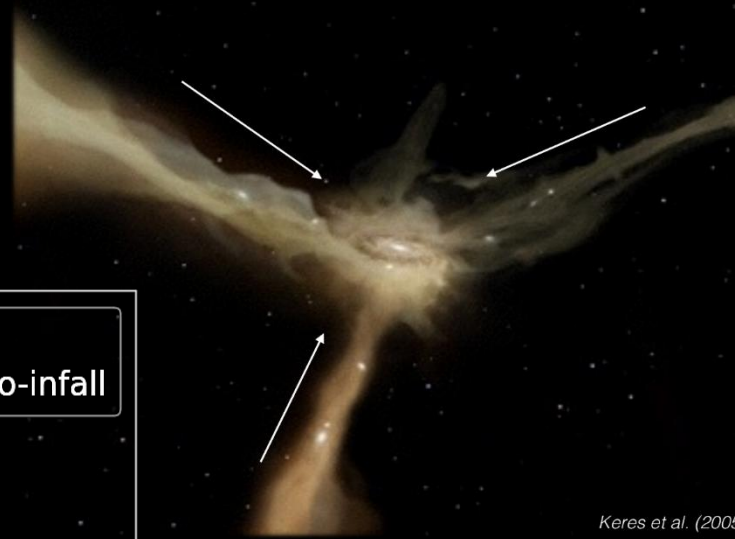
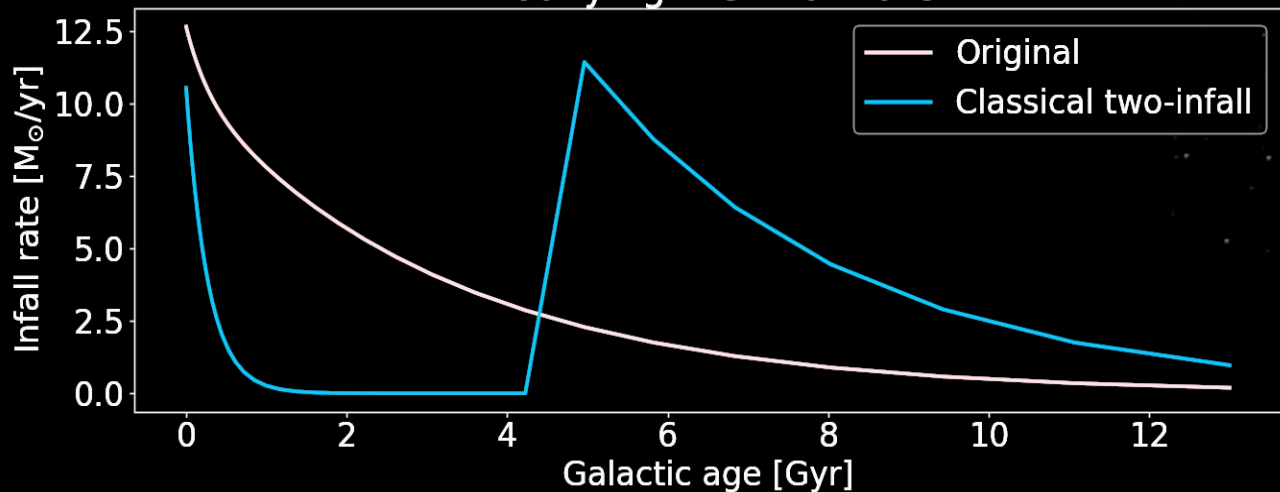
# The main equation



# 1. Gas inflow ( $dM_{in}$ )

- Composition: primordial, of Big Bang (? – not in interactions with another galaxy)
- Form of function:
  - Exponential decay  $dM_{in} = dM_{in,0} \cdot e^{-t/\tau}$
  - Two-infall

Modifying the infall rate



## 2. New stars ( $dM_*$ )

- **Stellar birthrate function:**

how many stars are born in the interval  $(t, t+dt)$  and  $(m, m+dm)$

- Star formation rate \* initial mass function

- **Star formation rate:** total mass of gas locked into new stars in a timestep

- Schmidt–Kennicutt law ( $k \approx 1,5$ )  $\dot{M}_*(t) = \nu \sigma^k(t)$

$\nu$ : star formation efficiency

$\sigma$ : surface mass density of gas

- **Initial mass function (IMF):**

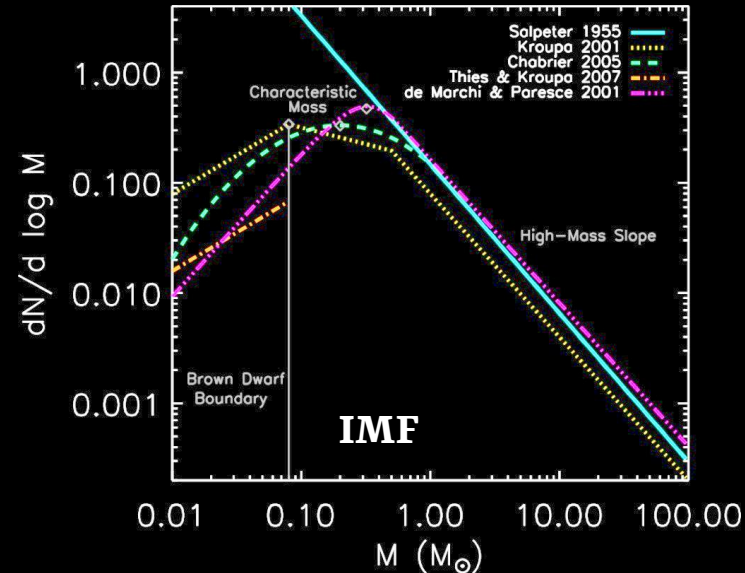
how many stars form between  $m$  and  $(m+dm)$

- Empirical forms (Salpeter, Kroupa)

- General form:  $\phi(m) dm = C m^{k'} dm$

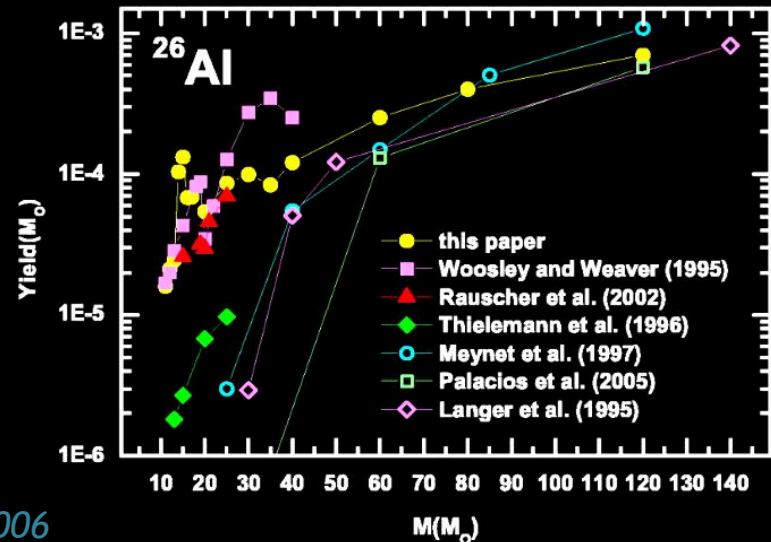
- Kroupa:

$$\phi(m) dm = n \cdot m^{-\alpha}, \begin{cases} n = 0,035; \alpha = 1,3 & m < 0,5 M_{\odot} \\ n = 0,019; \alpha = 2,2 & 0,5 M_{\odot} \leq m < 1 M_{\odot} \\ n = 0,019; \alpha = 2,7 & 1 M_{\odot} \leq m \end{cases}$$



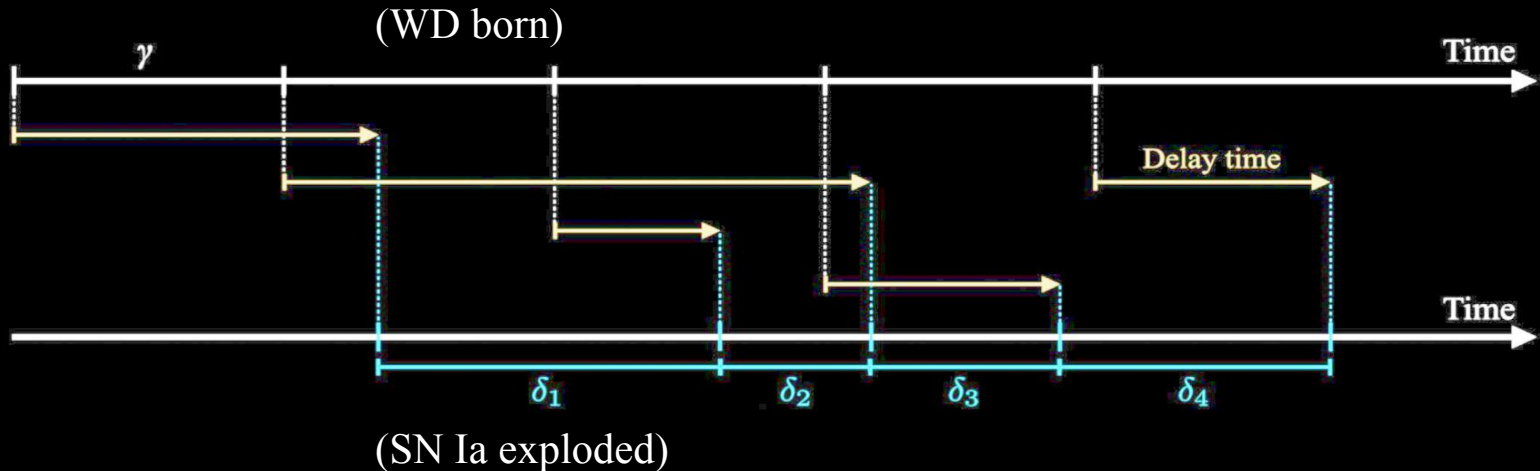
### 3. Recycled mass from stars ( $dM_{\text{rec}}$ )

- **Yield:** How much mass of an isotope is returned back by the stars
- Unprocessed + newly synthesized material
- Tables for stars of different masses, based on stellar nucleosynthesis models
- Uncertainties: nuclear physics, stellar structure models (convection), winds ...
- Depends on the mass of the current stars



# The rate of SNe Ia

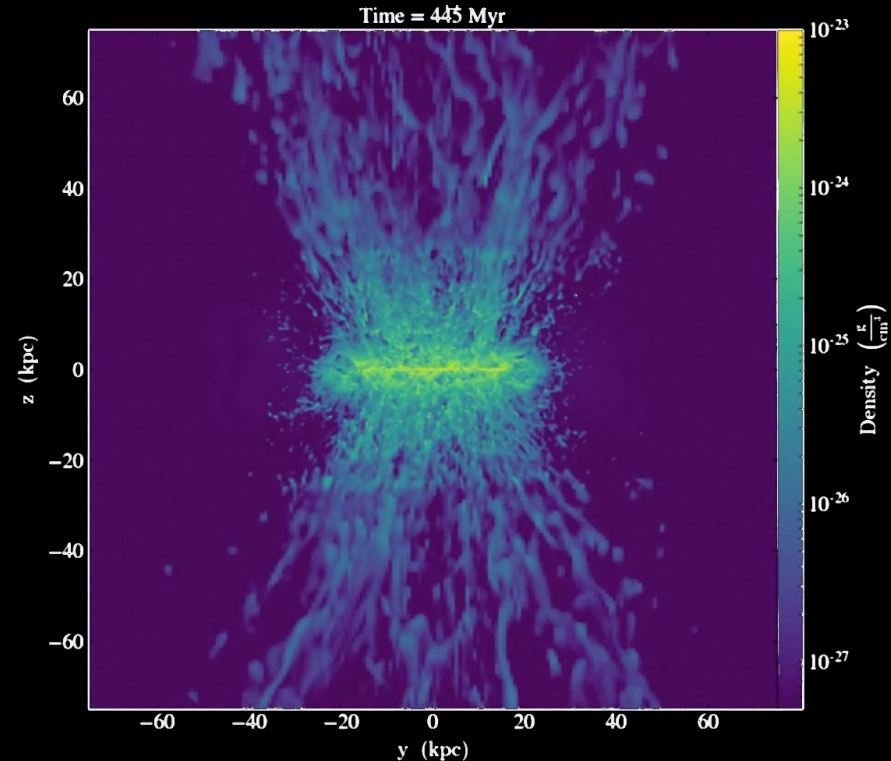
- Main synthesizer of iron
- The explosion occurs at different times after the white dwarf is created
- **DTD**, Delay time distribution:
  - Prompt/tardy SN Ia: exploded in 100 Myr or not





## 4. Gas outflows ( $dM_{\text{out}}$ )

- Gas outflows: driven by dynamics  $\rightarrow$  proportional to stellar formation
  - Young stars: winds, magnetic field
  - Mass loading  $\eta$ :  $dM_{\text{out}} = \eta \cdot dM_{\text{star}}$
- Radial flows
  - Flows inwards
  - Driven by the low angular momentum of infalling material
  - Contributes to the gradients in composition

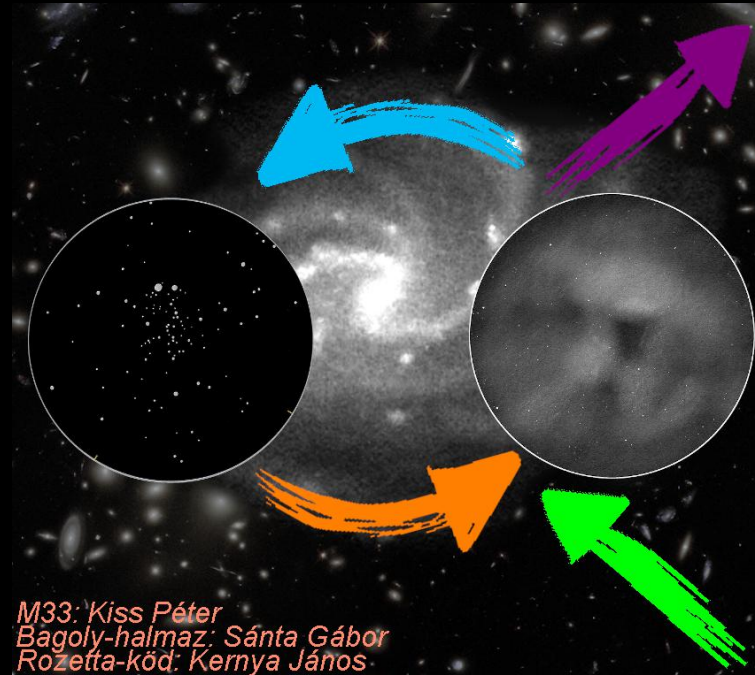


# The most important parameters

- Initial mass of the gas
- Rate of inflows and outflows
- Star formation rate, initial mass function - distribution of stars born
- Number density of supernovae
- Element production of stars with different masses (yields)

# The main equation: summary

- The change of mass of the gas:  $dM_{\text{gas}} = dM_{\text{in}} - dM_{*} + dM_{\text{rec}} - dM_{\text{out}}$ 
  1.  $dM_{\text{in}}$  exponentially decaying inflows
  2.  $dM_{*}$  star formation rate \* initial mass function
  3.  $dM_{\text{rec}}$  yields of stars; delay times for SN Ia
  4.  $dM_{\text{out}}$  gas outflows, by stars newly born
- True independently for all isotopes



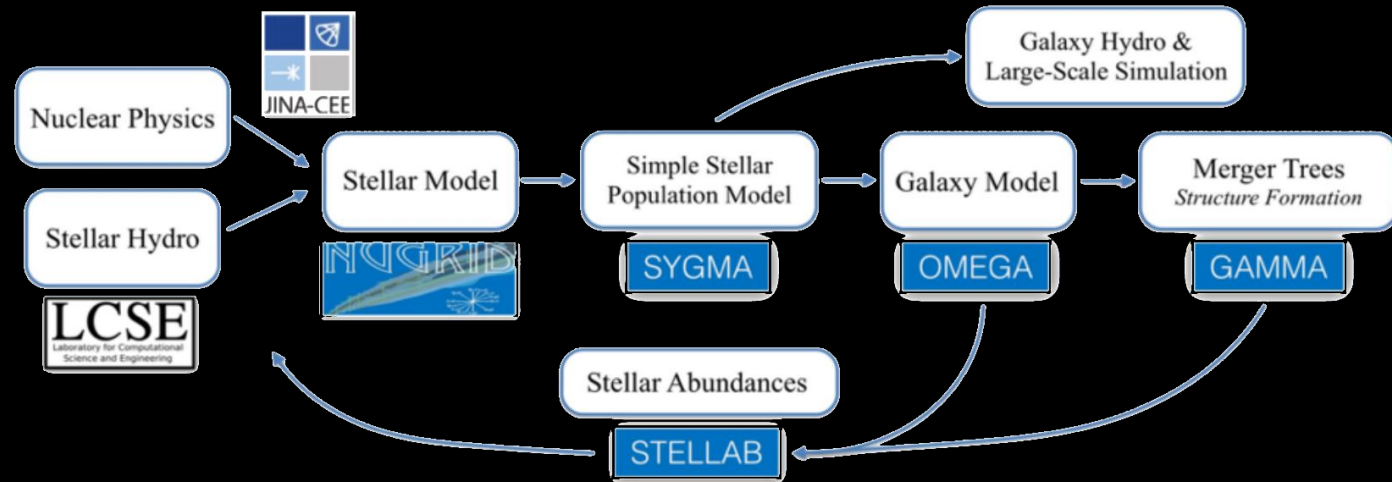
**OMEGA+**

# OMEGA

- OMEGA = One-zone Model for the Evolution of Galaxies
  - NuPyCEE package
  - <https://github.com/NuGrid/NUPYCEE>
- User-friendly, quick, but valuable GCE simulations

# Libraries of OMEGA

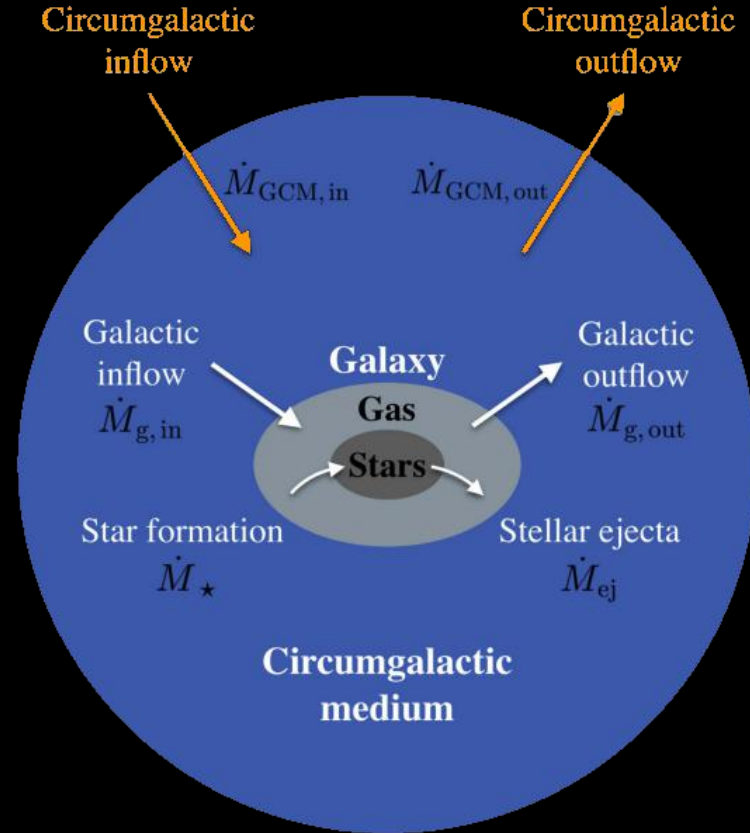
- Input: nuclear physics, stellar simulations
- SYGMA: evolution of one stellar population
- OMEGA: the galaxy model itself
- GAMMA: for mergers
- STELLAB: stellar abundances built-in, ready to compare with OMEGA!





# OMEGA+

- OMEGA+
  - Uses NuPyCEE for OMEGA
  - +: JinaPyCEE
  - <https://github.com/becot85/JINAPyCEE>
- Two zones:
  - The galaxy itself, see OMEGA
  - + Hot gas reservoir (From here, the material can fall back)



**Let's get down to the notebook! Have fun!**

If you have any questions, either about the material or the installation,  
don't hesitate to contact me: [blanka.vilagos@astro.su.se](mailto:blanka.vilagos@astro.su.se)